

Two-meson cloud contribution to the baryon antidecuplet self-energy

T. Hyodo^a, A. Hosaka^a, F.J. Llanes-Estrada^b, E. Oset^c, J. R. Peláez^d and
M. J. Vicente Vacas^c,

^aResearch Center for Nuclear Physics (RCNP), Ibaraki, Osaka 567-0047, Japan.

^bUniversidad Complutense de Madrid, Depto. Física Teórica I, 28040 Madrid, Spain.

^cDepartamento de Física Teórica and IFIC, Centro Mixto Universidad de Valencia-CSIC, Institutos de Investigación de Paterna, Aptd. 22085, 46071 Valencia, Spain.

^dUniversidad Complutense de Madrid, Depto. Física Teórica II, 28040 Madrid, Spain.

We study the self-energy of the $SU(3)$ antidecuplet coming from two-meson virtual clouds. Assuming that the exotic Θ^+ belongs to an antidecuplet representation with $N(1710)$ as nucleon partner, we derive effective Lagrangians that describe the decay of $N(1710)$ into $N\pi\pi$ with two pions in s - or p -wave. It is found that the self-energies for all members of the antidecuplet are attractive, and the larger strangeness particle is more bound. From two-meson cloud, we obtain about 20% of the empirical mass splitting between states with different strangeness.

1. Introduction

In recent years, the study of the exotic pentaquark baryons has been one of the most exciting fields. Evidence of exotic Θ^+ was reported in Ref. [1] and a signal of another exotic state Ξ^{--} was subsequently observed [2], though the experimental confirmation of the latter is somehow controversial. In hadron spectroscopy, the Gell-Mann–Okubo[GMO] formula has been successfully applied to describe the mass splitting of particles within an $SU(3)$ multiplet. The smallest multiplet containing Θ^+ and Ξ^{--} is the antidecuplet ($\overline{10}$), and equal mass splitting is obtained from the GMO rule. Here we would like to study the two-meson cloud effect to the baryon antidecuplet, which would contribute to mass splitting in addition to the GMO formula.

The study of the two-meson cloud effect is motivated by the attempts of constructing the Θ^+ as a $K\pi N$ bound state [3, 4, 5, 6], in which an attractive interaction is found for the $K\pi N$ states of $J^P = 1/2^+$. Although the found attraction is not enough to bind the three body system, such a configuration is naturally expected in the Θ^+ structure, by observing that the $K\pi N$ mass is only 30 MeV above the Θ^+ state.

In the present work, assuming that the $N(1710)$ has a large antidecuplet component, we construct flavor $SU(3)$ effective interaction Lagrangians, which account for the decay modes of the $N(1710)$ into $N\pi\pi$. Using these interaction Lagrangians, we calculate the self-energy of the antidecuplet. Details of the study can be found in Ref. [7].

2. Formulation

The interaction Lagrangians are constrained to be $SU(3)$ symmetric. The process we are considering is $\mathbf{8}_M + \mathbf{8}_M + \mathbf{8}_B \rightarrow \mathbf{10}_P$, where we denote the octet baryon, meson and antidecuplet baryon as $\mathbf{8}_B$, $\mathbf{8}_M$ and $\mathbf{10}_P$, respectively. In order to construct a singlet from the product of $\mathbf{8}_M$, $\mathbf{8}_M$, $\mathbf{8}_B$, and $\mathbf{10}_P$, there are four combinations, in which two $\mathbf{8}_M$ mesons are combined into $\mathbf{8}_{MM}^s$, $\mathbf{8}_{MM}^a$, $\mathbf{10}_{MM}$ and $\mathbf{27}_{MM}$. However, two of them ($\mathbf{8}_{MM}^a$, $\mathbf{10}_{MM}$) are identically zero, due to additional symmetry under exchange of two mesons. Hence, without using derivatives, we can construct the following effective Lagrangians:

$$\mathcal{L}^{8s} = \frac{g^{8s}}{2f} \bar{P}_{ijk} \epsilon^{lmk} \phi_l^a \phi_a^i B_m^j + h.c. , \quad (1)$$

$$\mathcal{L}^{27} = \frac{g^{27}}{2f} \left[4 \bar{P}_{ijk} \epsilon^{lbk} \phi_l^i \phi_a^j B_b^a - \frac{4}{5} \bar{P}_{ijk} \epsilon^{lbk} \phi_l^a \phi_a^j B_b^i \right] + h.c. , \quad (2)$$

where P , B and ϕ are the baryon antidecuplet, baryon octet and meson octet fields, respectively. We have included a factor $1/2f$ to make g^{8s} and g^{27} dimensionless ($f = 93$ MeV is the pion decay constant). In the low momentum expansion, the above Lagrangians are the two lowest ones. In practice, however, they are not sufficient to account for the experimental decay of $N(1710)$ into $N\pi\pi$ (p -wave). In order to reproduce such decay mode, we introduce a Lagrangian with one derivative:

$$\mathcal{L}^{8a} = i \frac{g^{8a}}{4f^2} \bar{P}_{ijk} \epsilon^{lmk} \gamma^\mu (\partial_\mu \phi_l^a \phi_a^i - \phi_l^a \partial_\mu \phi_a^i) B_m^j + h.c. . \quad (3)$$

We will address other possible interaction Lagrangians [7] later on.

The antidecuplet self-energies are given by

$$\Sigma_P^{(j)}(p^0) = \sum_{B, m_1, m_2} \left(F^{(j)} C_{P, B, m_1, m_2}^{(j)} \right) I^{(j)}(p^0; B, m_1, m_2) \left(F^{(j)} C_{P, B, m_1, m_2}^{(j)} \right) , \quad (4)$$

where the index j labels the interaction Lagrangians, p^0 is the energy of the antidecuplet baryon, $F^{(j)}$ are coupling constants appearing in the Lagrangian, and $C_{P, B, m_1, m_2}^{(j)}$ are $SU(3)$ coefficients which are compiled in the Appendix of Ref. [7]. The function $I^{(j)}(p^0; B, m_1, m_2)$ is the two-loop integral with two mesons and one baryon (Fig. 1, left):

$$\begin{aligned} & I^{(j)}(p^0; B, m_1, m_2) \\ &= - \int \frac{d^4 k}{(2\pi)^4} \int \frac{d^4 q}{(2\pi)^4} |t^{(j)}|^2 \frac{1}{k^2 - m_1^2 + i\epsilon} \frac{1}{q^2 - m_2^2 + i\epsilon} \frac{M}{E} \frac{1}{p^0 - k^0 - q^0 - E + i\epsilon} , \end{aligned} \quad (5)$$

where $t^{(j)}$ are the amplitudes derived from the Lagrangian j , M and m_i are the masses of a baryon and mesons, E is the energy of the intermediate baryon. The real part of this integral is cut off with a three momentum Λ in the range 700-800 MeV. The imaginary part of the diagram provides the decay width.

It is known that $N(1710) \rightarrow N\pi\pi$ (p -wave) occurs through the $N\rho$ decay, therefore, we improve the contact interaction of the \mathcal{L}^{8a} to account for the vector meson propagator (Fig. 1, right), including the factor $m_v^2/[(q+k)^2 - m_v^2]$ in each $P \rightarrow BMM$ vertex.



Figure 1. Diagrams for self-energy of baryon antidecuplet due to two-meson cloud. Right : inclusion of vector meson propagator.

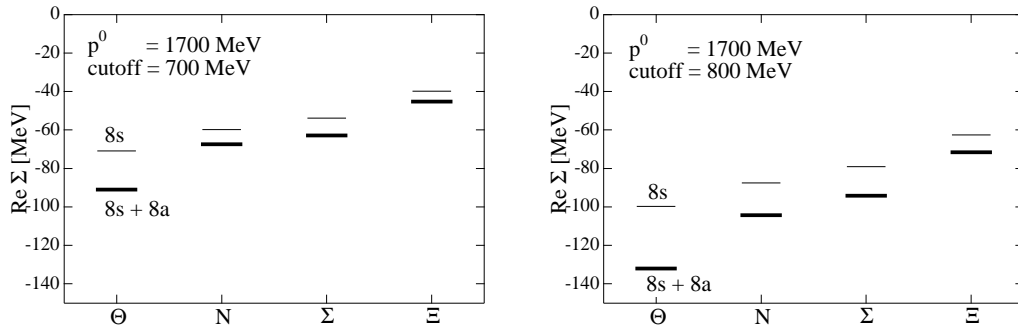


Figure 2. Mass shifts of baryon antidecuplet ($\text{Re}\Sigma_P$) with $p^0 = 1700$ MeV.

3. Numerical results

Here we show the results with \mathcal{L}^{8s} and \mathcal{L}^{8a} . \mathcal{L}^{27} and other possible Lagrangians will be addressed later. The parameters g^{8s} and g^{8a} are fixed so as to obtain the partial decay widths of the $N(1710)$ to $N\pi\pi$ (s -wave, isoscalar) and $N\rho \rightarrow N\pi\pi$ (p -wave, isovector) respectively. The central values in the PDG [8] are 25 and 15 MeV, which correspond to $g^{8s} = 1.9$ and $g^{8a} = 0.32$, respectively. We take an average value of $p^0 = 1700$ MeV as input. The qualitative trend of the result does not depend on the p^0 , but the magnitude of the self-energy is changed [7].

In Fig. 2 we show the real parts of the self-energies for the contributions from \mathcal{L}^{8s} and total contributions of \mathcal{L}^{8a} and \mathcal{L}^{8s} , with cutoffs 700 and 800 MeV. We see that all the self-energies are attractive, and that the interaction is more attractive the larger the strangeness. \mathcal{L}^{8s} provides more binding than \mathcal{L}^{8a} for the same cutoff. The splitting between the $\Theta_{\bar{10}}$ and $\Xi_{\bar{10}}$ states is about 45-60 MeV depending on the cutoff. Since the experimental splitting of the $\Theta(1540)$ and $\Xi(1860)$ is 320 MeV, the two-meson cloud provides 20% of the total splitting. This should be compared to 60% naturally provided by the mass of the constituent strange quarks, which would leave about 20% more for the effects of quark correlations.

The partial decay widths are shown in Table 1. We have taken the observed masses $M_{N_{\bar{10}}} = 1710$, $M_{\Sigma_{\bar{10}}} = 1770$ and $M_{\Xi_{\bar{10}}} = 1860$ MeV as p^0 , because the phase space is essential for the decay width. We can see that the widths are not very large for all channels. Indeed, $\Sigma(1770)$ and $\Xi(1860)$ would have widths for three body channels of about 24 and 2 MeV, which are compatible with the experimental total width of about 70 and 18 MeV, respectively [2, 8]. Detailed information of the partial decay widths of

Table 1

Partial decay widths for the allowed channels and total width for any BMM channel, at the masses of the antidecuplet members. All values are listed in units of MeV.

Decay widths [MeV]	$\Gamma^{(8s)}$	$\Gamma^{(8a)}$	Γ_{BMM}^{tot}
$N(1710) \rightarrow N\pi\pi$ (inputs)	25	15	40
$N(1710) \rightarrow N\eta\pi$	0.58	-	
$\Sigma(1770) \rightarrow N\bar{K}\pi$	4.7	6.0	24
$\Sigma(1770) \rightarrow \Sigma\pi\pi$	10	0.62	
$\Sigma(1770) \rightarrow \Lambda\pi\pi$	-	2.9	
$\Xi(1860) \rightarrow \Sigma\bar{K}\pi$	0.57	0.46	2.1
$\Xi(1860) \rightarrow \Xi\pi\pi$	-	1.1	

three body channels will give us more understanding of the interaction Lagrangian.

In Ref [7], apart from the above Lagrangians and a \mathcal{L}^{27} term, we also considered the leading order Lagrangians in a chiral expansion as dictated by QCD. There are two terms: one chirally symmetric and a mass term. The latter has to be tiny since it violates SU(3). The former gives similar results to \mathcal{L}^{8s} . The role of chiral symmetry is thus small and the use of \mathcal{L}^{8s} is justified.

4. Summary

We study the self-energy of the baryon antidecuplet due to the two-meson cloud. The assumptions made throughout the paper and the uncertainties in the experimental input make the nature of our analysis qualitative. However, in all different cases studied, the two-meson cloud mechanism leads to the following conclusions: An attractive self-energy is obtained for all members of the antidecuplet. The two-meson cloud contributes to the mass splitting between antidecuplet members about 20% of the empirical one. These observations are consistent with the previous attempts to describe the Θ^+ as a $K\pi N$ state [3, 4, 5, 6], and the magnitude of 20% is also in agreement quantitatively with the strength of attraction [5]. The role played by the two-meson cloud is therefore of relevance for a precise understanding of the nature of the Θ^+ and the antidecuplet.

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